

## AE6170 Structural Optimization

Prerequisites: Graduate Standing and/or Consent of Instructor

Course Listing: Mathematical methods of constrained optimization, sensitivity analysis, approximation concepts, decomposition techniques, shape optimization in the context of structural design.

### **1. Mathematical Statement of the Structural Optimization Problem (1 hour)**

Definition and classification of constraints  
Solution process  
Analysis and design formulations

### **2. Classical Optimization Using Calculus of Variations (3 hours)**

Applications to beams of maximum strength  
Columns and vibrating structures

### **3. Linear Programming, Simplex Method, Duality (5 hours)**

Application to limit design of trusses and frames

### **4. Nonlinear Optimization - Use of Linear Programming for Solving (Nonlinear) Structural Optimization Problems (5 hours)**

Separable programming  
Stewart and Griffith's method  
Kelley's cutting plane method

### **5. Unconstrained Optimization as a Prelude to Nonlinear Constrained Optimization (6 hours)**

Conjugate directions method  
Gradient methods

### **6. Kuhn-Tucker Conditions for Optimality (2 hours)**

Computations of Lagrange multipliers

### **7. Gradient Projection and Reduced Gradient Methods (2 hours)**

Applications to solving structural optimization problems

### **8. Method of Feasible Directions (5 hours)**

Applications to solving structural optimization problems

### **9. Penalty Method - Exterior and Interior Penalty Functions (2 hours)**

Quadratic and cubic extended penalty functions  
Use of SUMT (Fiacco-McCormack's sequential unconstrained minimization technique) for solving structural optimization problems

### **10. Introduction to Generalized Optimality Criteria and Dual Methods (4 hours)**

Connection between optimality criteria and mathematical programming

### **11. Sensitivity Analysis (7 hours)**

Direct and adjoint methods for sensitivity derivatives  
Approximation concepts

### **12. Recent Developments in Multilevel and Decomposition Techniques (3 hours)**

**13. Shape Optimization** (4 hours)

**Midterm Exam** (1 hour)

**Total** (45 hours)

Ref: *Elements of Structural Optimization* by R. Hafta, Z. Gurdal & M.P. Kamat

*Structural Optimization: Status & Promise*, Ed. M.P. Kamat